

ZAK TRANSFORM FOR BOEHMIANS

VASANT GAIKWAD¹ & M. S. CHAUDHARY²

¹Department of Mathematics, Shri Chhatrapati Shivaji College, Omerga, Maharashtra, India

²Department of Mathematics, Shivaji University, Kolhapur, Maharashtra, India

ABSTRACT

It is known that the classical Zak Transform is a linear unitary transformation from $L^2(\mathbb{R})$ onto $L^2(\mathbb{Q})$ whose image can be completely characterized. In this paper, we shall construct a Bohmian space B_1 containing $L^2(\mathbb{R})$ and another Bohmian space B_2 containing $L^2(\mathbb{Q})$ and define Zak transform as a continuous linear map of B_1 onto B_2 . We shall also prove that this extended definition is consistent with the classical definition and that there are Boehmians which are not L^2 – functions but for which we can define the generalized Zak transform.

KEYWORDS: Boehmians, Convolution, Lebesgue Measurable Functions, Sequence, and Zak Transform

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